



Games, Interactions and Networks

Giorgio Fagiolo

<https://mail.sssup.it/~fagiolo>

University of Verona, Verona, Italy

and

S.Anna School of Advanced Studies, Pisa, Italy



Outline of the Talk (1/2)

- Macro Order from Micro Disorder
- Examples:
 - How do market prices and interest rates emerge?
 - How do GNP, unemployment, consumption, investment move together along economic cycles?
 - How do some technological standards manage to dominate a market?
- Coordination and Technological Adoption
- Insights from Standard Models



Outline of the Talk (2/2)

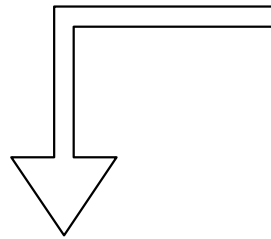
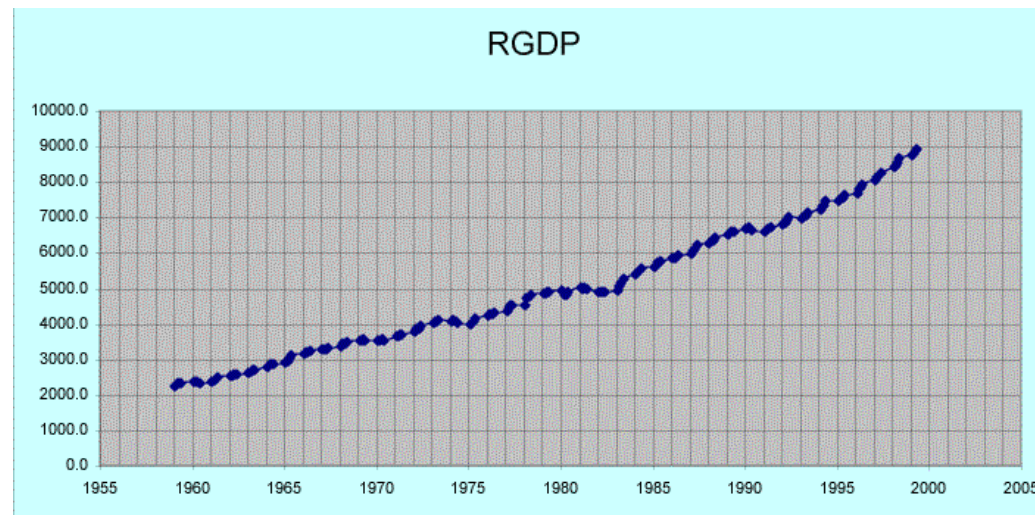
- Interactions, Networks and Adoption Choices
- Examples
 - How can networks help us in understanding technological adoption and diffusion?
- Conclusions



Macro Order from Micro Disorder (1/2)

- Economies and societies as complex systems
 - Micro Level (Firms, Consumers, Households, Individuals...)
 - Macro Level (Aggregate Variables, Macro Patterns, ...)
- Micro Level
 - Many entities interacting over time
 - Possibly conflicting interests
- Macro Level
 - Properties emerging from micro level
 - Feedback to micro level

Macro Order from Micro Disorder (2/2)



Feedback
to Micro
Level



Micro Level

- Firms competing in turbulent markets
- Undertaking strategic decisions (output, investments, marketing, R&D, innovation, etc.)

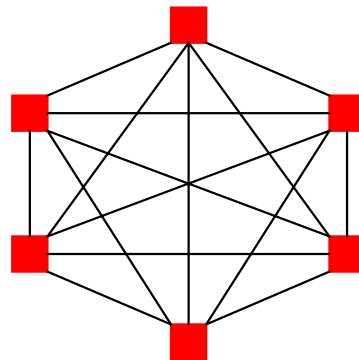


Macro Order: Coordination

- Coordination among individuals
 - Technological adoption between standards (PC vs. Mac, Unix vs. Windows, Qwerty vs. Dvorak, etc.)
 - Social norms (languages, currencies, etc.)
- Micro Level
 - Network externalities: my utility from choosing X increases in the number of agents choosing X
 - Coordination on a single technology in agents' interest
- Macro Level
 - Which technology will be adopted?
 - Why does one observe co-existence of standards?

Standard Answers: Game Theory (1/4)

- Common Setup: Two basic assumptions
 - Economic agents are perfectly rational
 - Maximize expected utility
 - Each agent “interacts” with anyone else
 - Individual utility depends on what every other single player does
- Interaction networks
 - Complete Network: every pair of agents is connected





Standard Answers: Game Theory (2/4)

- Coordination: Strategic complementarities
 - Two standards (Unix vs. Windows, Mac vs. PC)
 - Each individual has interest in doing what the other does

| | | | |
|--------|--------|----------|---|
| | | Opponent | |
| | Payoff | X | Y |
| Myself | X | 4 | 0 |
| | Y | 0 | 2 |



Standard Answers: Game Theory (3/4)

- Coordination: Strategic complementarities
 - Two standards (Unix vs. Windows, Mac vs. PC)
 - Each individual has interest in doing what the other does

| Payoff | | Opponent | |
|--------|---|----------|---|
| | | X | Y |
| Myself | X | 4 | 0 |
| | Y | 0 | 2 |



Standard Answers: Summary (4/4)

- Coordination will occur
 - Full coordination on one single technology should be the case
- Which technology will prevail?
 - We cannot predict
 - which technology will be selected
 - whether the “ex-ante” superior technology will emerge



A Critique: Three Basic Observations

- **Rationality.**
 - People are not fully rational
 - Make persistent mistakes, explore non-optimal options
- **Dynamics.**
 - Behaviors are often revised through time
 - Choices are based on observation of the past or “status quo”
- **Interactions.**
 - Agents do not typically care about any other single behavior
 - Interaction networks are far from being “complete”



Interaction Networks

- **Interactions: Basic Assumption**
 - Agents only care about a small subset of other agents
- **Significant others**
 - Friends, relatives, peers, neighbors, ...
 - Competitors, technologically-similar agents
- **Interaction networks are not complete**
 - Graph (links) describing who interacts with whom is sparse



Interaction Networks: Three Types

- **Type 1: Random Graphs**
 - Agents make a few random phone calls in each time period
- **Type 2: Local Interactions**
 - Agents always interact with their close friends
- **Type 3: Interaction Trees**
 - There are hierarchical relationships among agents



Interaction Networks (1/3)

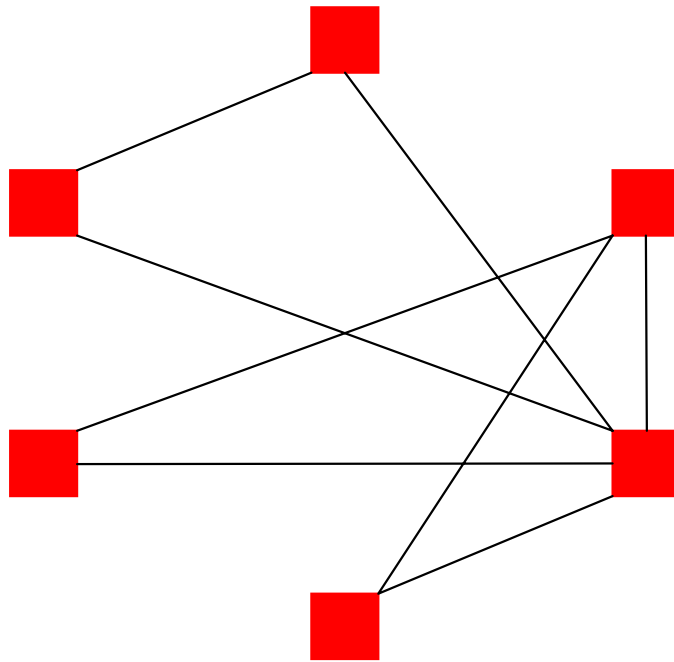
- **Interaction Networks as Random Graphs**
 - Agents make random phone-calls, search, meet people, etc.
 - No underlying geographical or social structure

- **Dynamics**
 - In each time period
 - any two agents in the population meet at random
 - agents tend to meet different **but few** people



Interaction Networks (1/3)

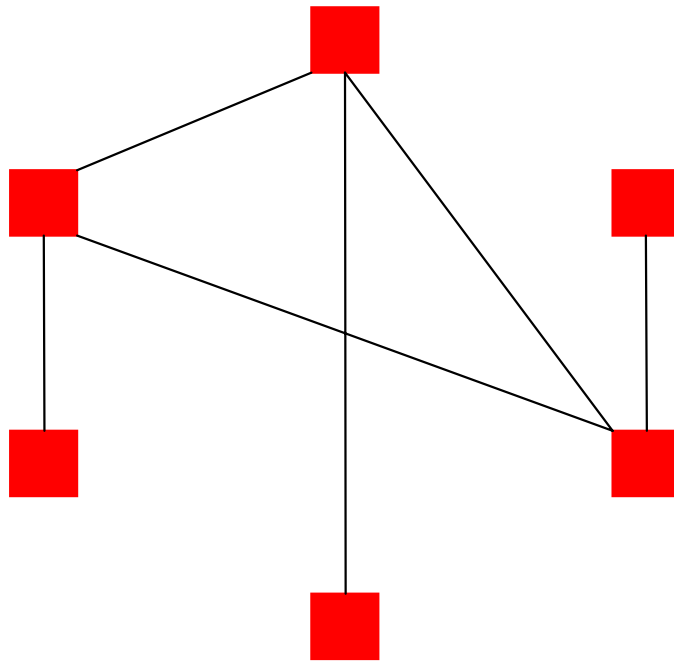
- **Dynamics of Random Graphs : $t=0$**





Interaction Networks (1/3)

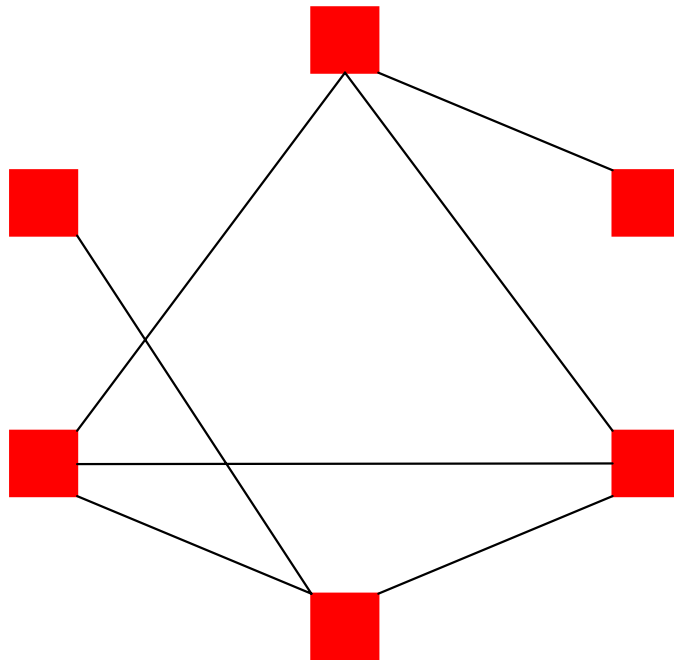
- **Dynamics of Random Graphs : $t=1$**





Interaction Networks (1/3)

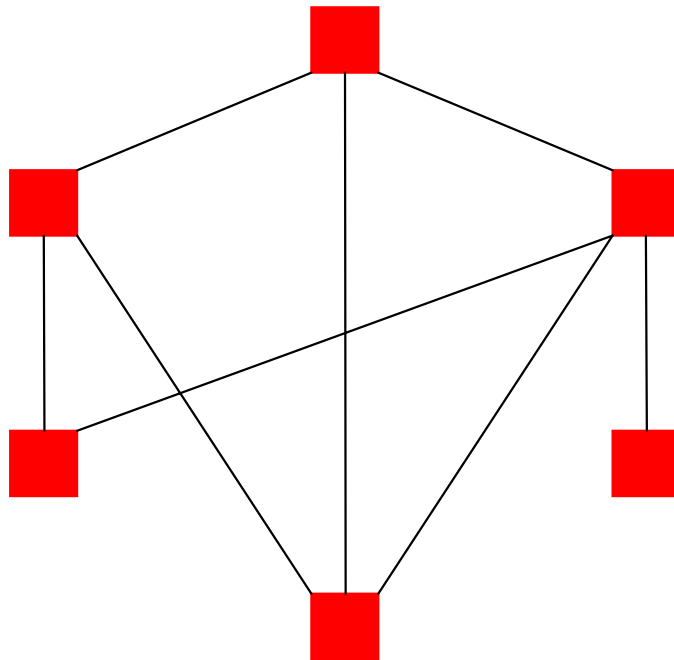
- **Dynamics of Random Graphs : $t=2$**





Interaction Networks (1/3)

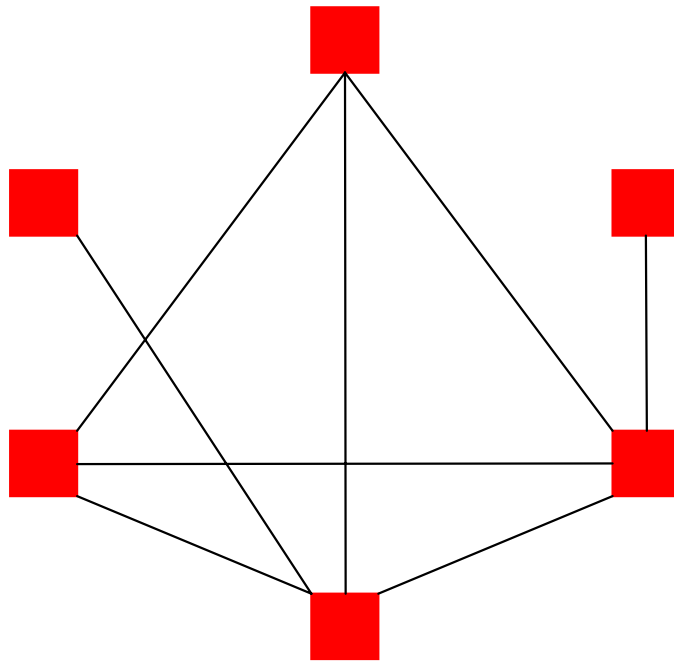
- **Dynamics of Random Graphs : $t=3$**





Interaction Networks (1/3)

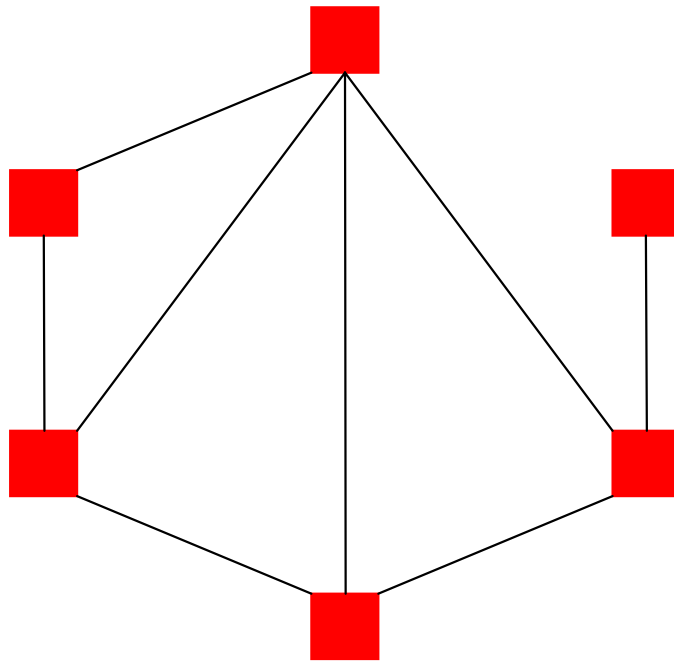
- **Dynamics of Random Graphs : $t=4$**





Interaction Networks (1/3)

- **Dynamics of Random Graphs : $t=5$... and so on ...**





Interaction Networks (2/3)

- **Random Graphs**

- Agents always switch interacting people
- Ok if switching (search) costs are small and there is no underlying spatial or social structure

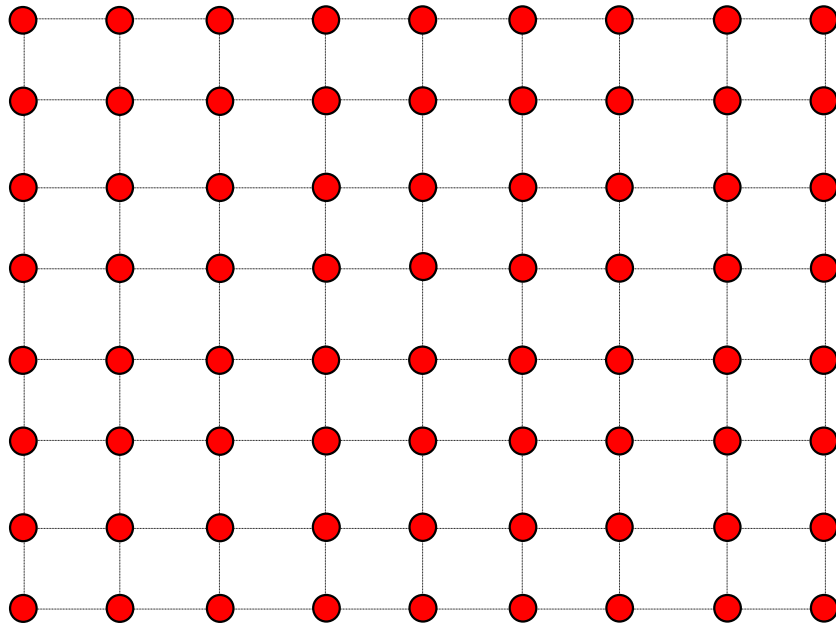
- **Alternative: Local Interactions**

- Friendships, neighboring relations, etc. can be sticky
- There is some underlying geographical (spatial) structure
- Agents always interact with their “nearest neighbors”



Interaction Networks (2/3)

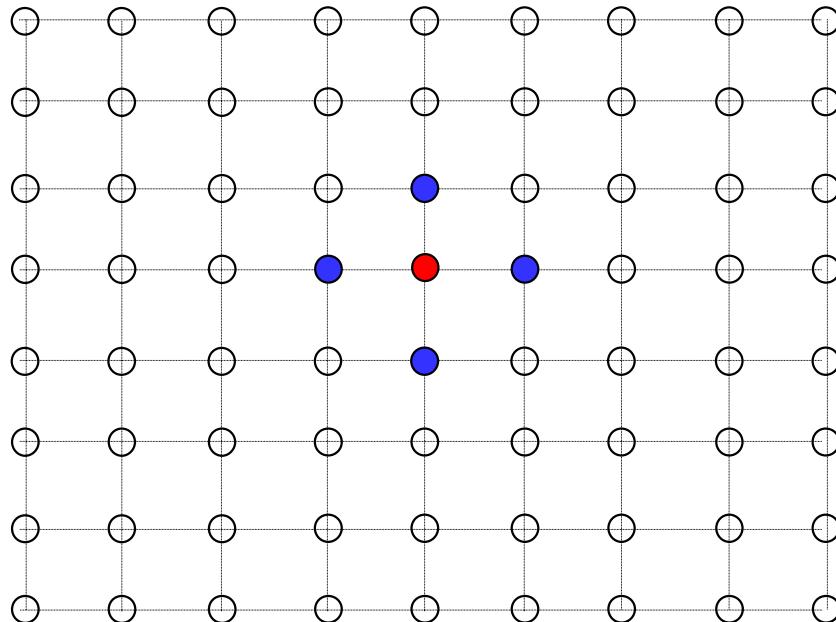
- **Local interactions: example**
 - Agents are thought to be arranged on a 2-dim lattice





Interaction Networks (2/3)

- **Local interactions: example**
 - Each interacts with his 4 nearest-neighbors



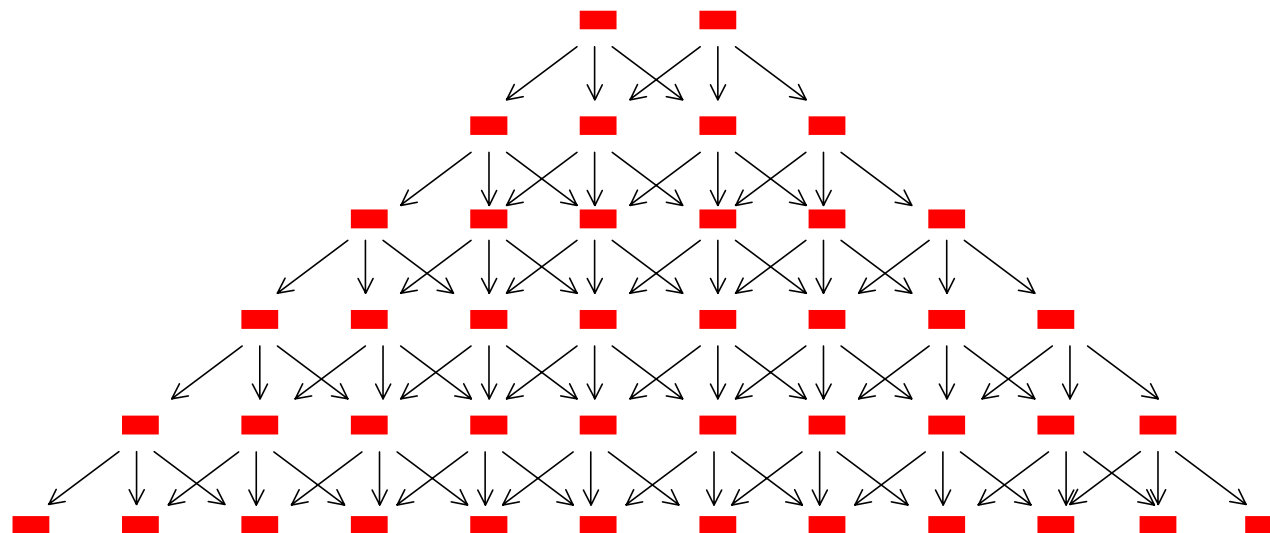
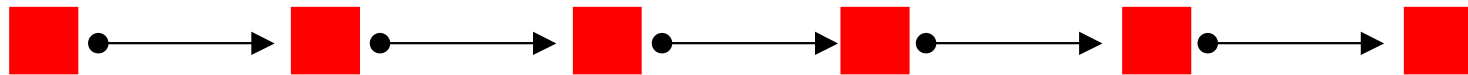


Interaction Networks (4/4)

- **Random graphs and local interactions**
 - No hierarchy whatsoever
 - Ok there is no information or role asymmetry among agents
- **Alternative: Interaction Networks as Trees**
 - Agents are not all the same as to their influence on others
 - Large firms can have advantages, upstream firms can move first
 - “Gurus” and “leaders” can force “followers” choices
 - There is some order in the way agents choose
 - Agents choosing
 - **first** face a higher uncertainty but are not influenced by others
 - **later** know what happened but are not free to choose

Interaction Networks (4/4)

- **Interaction networks as trees**





Our New Questions

- **What happens when**

- Real-world agents are not fully rational (mistakes, exploration)
- They are dynamically allowed to revise their choice through time
- They do so by taking into account only their “relevant others”

- **What do these new insights add to our understanding of**

- Aggregate coordination patterns generated out of micro level ?
- Prediction of:
 - Which technology (if any) will get the whole market (full coordination) ?
 - If and when “technological niches” will emerge (coexistence of techniques) ?



The Basic Setup

- **Agents**

- $i = 1, 2, \dots, 100$

- **Time**

- $t = 0, 1, 2, \dots$

- **Technologies**

- $S = \{A, B\}$
- $s(i, t)$: technology adopted by agent i at time t



Example I: Random Meetings (1/2)

- **Initial Conditions**

- 50 agents choosing A, 50 agents choosing B

- **Dynamics**

- At each t , two agents meet at random (only 1 phone call)
- The first agent asks the second which technology he uses
- Then the first agent:
 - With probability p : sticks to his previous choice
 - With probability $1-p$: adopts the technology suggested by the second

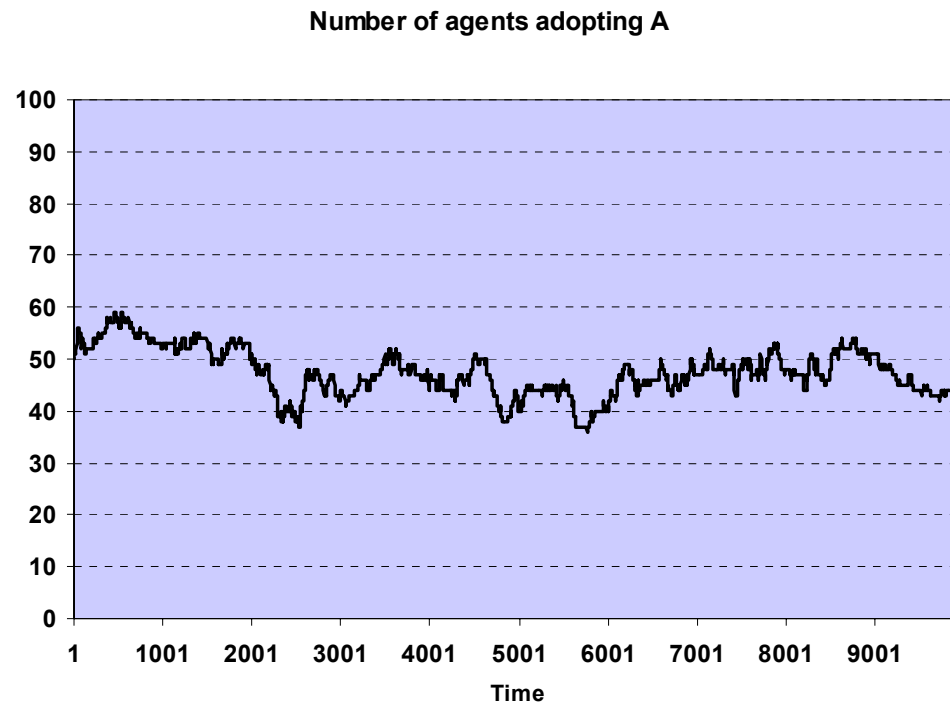
- **Remarks**

- Interaction networks are random
- The smaller p , the more agents are sensible to others' opinions

Example I: Random Meetings (2/2)

- **Results: Two cases**

- Large p (agents are "idiosyncratic"): **almost exact coexistence**

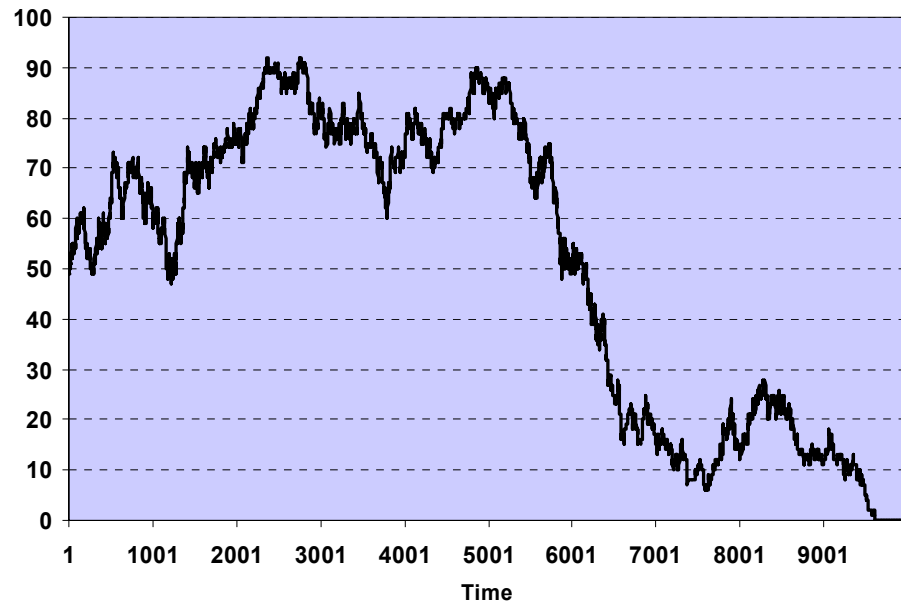


Example I: Random Meetings (2/2)

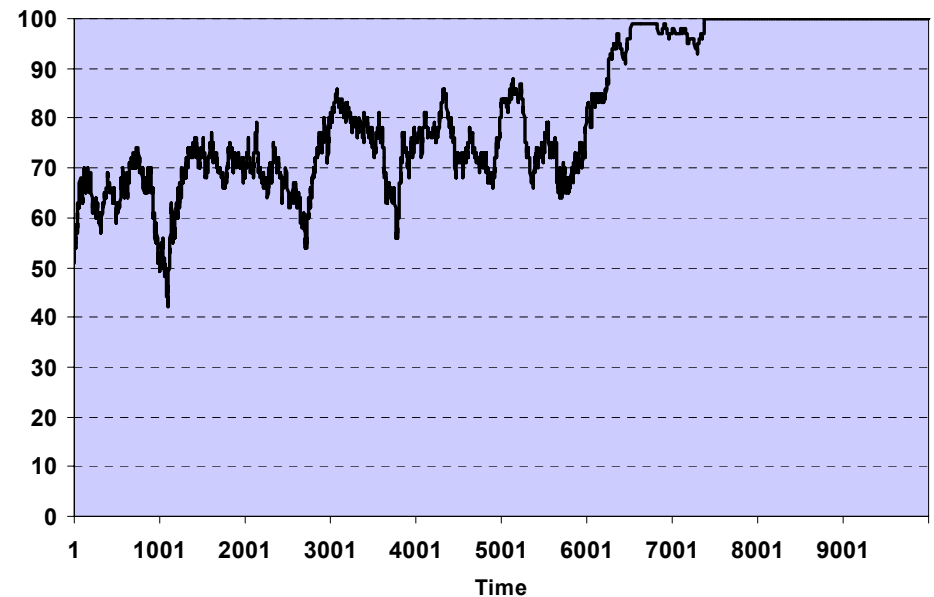
- **Results: Two cases**

- Small p (agents are sensible): **one technology wins**

Number of agents adopting A



Number of agents adopting A





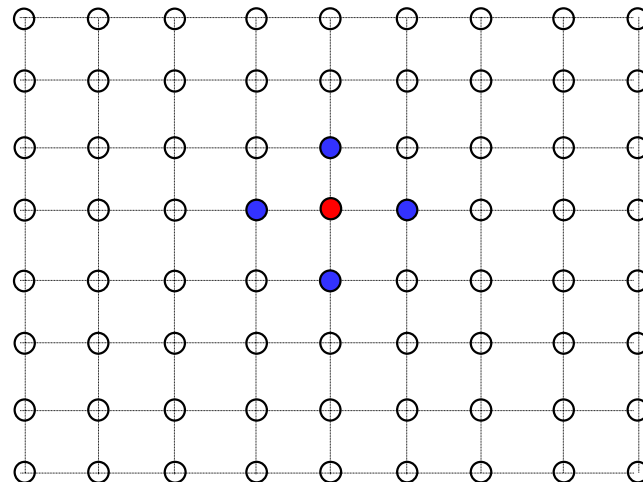
Example II: Local Interactions (1/3)

- **Initial Conditions**

- 50 agents choosing A, 50 agents choosing B

- **Interaction Networks**

- Agents are spatially located on a 2-dim lattice
- They only care about their 4 nearest-neighbors





Example II: Local Interactions (2/3)

- **Dynamics**

- At each t , one agent chosen at random is allowed to revise
- The agent looks at which technology prevails in his neighborhood
- He chooses the locally prevailing technology
- With some probability p he changes his mind and chooses the other technology (mistake or experimentation)

- **Remarks**

- Interaction networks are fixed
- The smaller p , the more agents are sensible to others' opinions

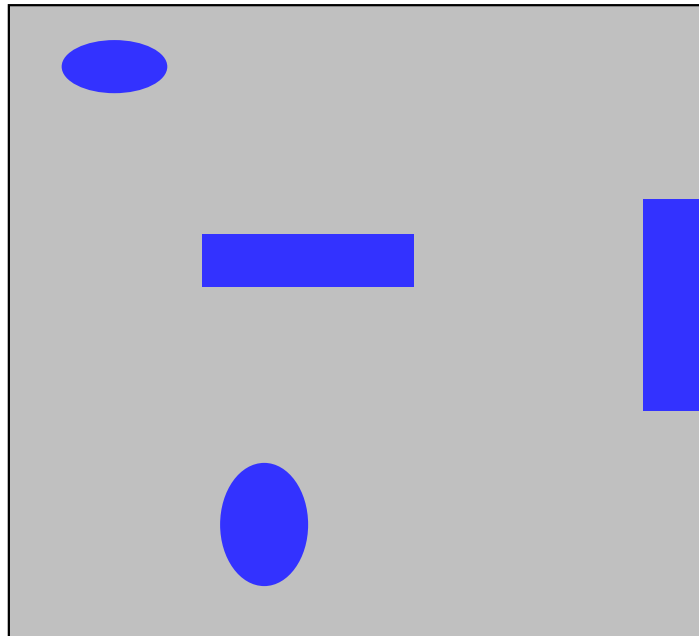
Example II: Local Interactions (3/3)

■ **Result I**

- Similar to before as to how p affects dynamics
- For small p , technological niches remain in the system
- **No technology gets the whole market**

Blue: Tech A

Grey: Tech B





Example II: Local Interactions (3/3)

■ Result II

- Can we predict winning technology? No answers so far
 - Here: The one associated to highest **average** payoffs will prevail
- **This is not necessarily the Pareto-efficient one !**

| | | Neighbor | |
|--------|---|----------|---|
| | | A | B |
| Myself | A | 4 | 0 |
| | B | 0 | 2 |

| | | Neighbor | |
|--------|---|----------|----|
| | | A | B |
| Myself | A | 4 | -3 |
| | B | 0 | 2 |



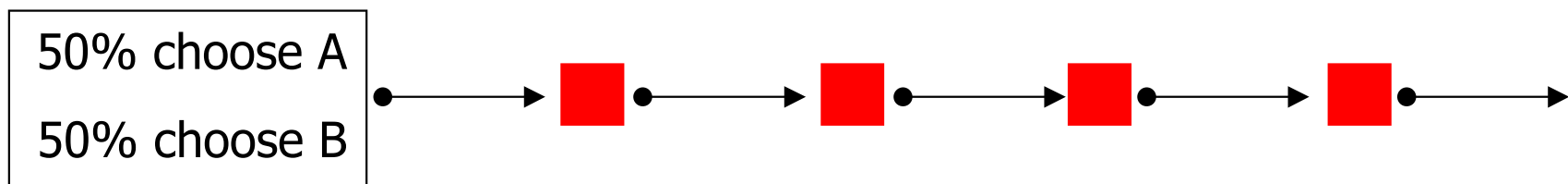
Example III: Tree Networks (1/4)

- **Initial Conditions**

- Small number of agents
- 50% agents choosing A, 50% agents choosing B

- **Interaction Networks**

- Agents choose sequentially
- They stick to their choices once they have chosen
- When choosing, they look at current number of adopters of A,B





Example III: Tree Networks (2/4)

- **Dynamics**

- At each t , one agent enters the economy
- He acquires information about prevailing technology
- He chooses prevailing technology
- With some probability p he changes his mind and chooses the other technology

- **Remarks**

- Interaction networks are fixed and sequential
- The smaller p , the more agents are sensible to others' opinions
- Agents choosing late are not able to change relative frequencies of adopters



Example III: Tree Networks (3/4)

- **Early choices (leaders)**

- Agents choosing first face higher uncertainty
 - They do not know which technology will prevail
 - Choices are partly random and idiosyncratic
- Their early choices make one technology better than the other
 - The gap between adopters increases in the early stages
 - They “build” the gap and “set the trend” to be followed afterwards

- **Late choices (followers)**

- Agents choosing late face low uncertainty
 - They can see which technology is prevailing
- Their choices **cannot** displace the “status quo”
 - The gap between adopters is already large
- They will tend to **follow the herd**



Example III: Tree Networks (4/4)

- **Result 1**

- One technology will (almost) get the whole market
- Which one will be is unpredictable

- **Result 2**

- Which technology will prevail is determined by “leaders” choices, which are partly random

- **Result 3**

- Followers choices are almost completely predetermined by leaders
- Informational cascade: followers do not use their information or freedom (fundamentals may not count)



Summary

- **Interaction, Networks and Adoption Choices**

- **Question**

- How can networks help us in understanding technological adoption and diffusion?

- **Answers**

- Non-trivial interaction networks help us in addressing issues as:
 - Can one technology get the whole market?
 - Can one explain coexistence of techniques and niches?
 - Which technology will tend to prevail?
 - What is the role of information asymmetries (leaders/followers)



Concluding Remarks

- **Interaction Networks: Additional Applications**

- Cooperation
- Financial bubbles
- Credit market, systemic risk
- [...]

- **Interaction Networks: Current research topics**

- This lecture: agents cannot choose whom to interact with
- What if agents can choose their interaction networks?
- Interesting questions:
 - Can we explain observed real-world interaction networks
 - Small-world, scale-free, etc. ?